

## Middle School Mathematics Contest – 2017 Solution Key

(Students may have alternate strategies for finding the solutions.)

### Non-Calculator Section Answers

(1) **12<sup>th</sup>** floor;  $14 + 6 + -4 + 8 + -5 + 2 + -9 = 12$

(2) **3  $\frac{3}{4}$  servings**;  $1 \frac{1}{2} \div \frac{2}{5} = \frac{3}{2} \times \frac{5}{2} = \frac{15}{4} = 3 \frac{3}{4}$  servings

(3) **IQR = 18**; first, arrange the scores in order:

49, 52, 53, 54, 55, 61, 63, 64, 65, 66, 70, 71, 74, 78, 81, 84; for the median, there are two scores in the middle, 64 and 65 so 64.5 is the median; the middle of the lower half has two scores in the middle, 54 and 55 so 54.5 is the lower quartile; the upper half has two scores in the middle, 71 and 74 so 72.5 is the upper quartile; the IQR = upper quartile 72.5 – lower quartile 54.5; the IQR = 18.

(4) **12%**;  $\$94.99 - \$83.99 = \$11$ ;  $11 \div 94.99 \times 100 = 11.58\dots$  which rounds to 12%.

(5) **117**; using Order of Operations:  $[(10 - 5)^2 + 24 \div 2^3 \times 5 - 7^0] \div \frac{1}{3}$

$$[(5)^2 + 24 \div 2^3 \times 5 - 7^0] \div \frac{1}{3} = [25 + 24 \div 8 \times 5 - 1] \div \frac{1}{3}$$

$$[25 + 3 \times 5 - 1] \div \frac{1}{3} = [25 + 15 - 1] \div \frac{1}{3}$$

$$[40 - 1] \div \frac{1}{3} = [39] \div \frac{1}{3}$$

$$[39] \div \frac{1}{3} = 39 \times \frac{3}{1}$$

$$= 117$$

(6) **angle x = 57 ° ; angle k = 17 ° ; angle m = 54 ° ; angle w = 72 ° ; angle y = 18 °**

(7) (a) The greatest number of bracelets is **15**; find the greatest common factor of 75 and 90 which is 15; (b) for the beads of each type:  $75 \div 15 = 5$  **gemstones** and  $90 \div 15 = 6$  **crystals**.

(8) **-39**; substitute  $r = 3$ ,  $w = -5$ , and  $h = -4$  in the expression:

$$[(w - r)^2 + rh] \div h/r$$

$$[(-5 - 3)^2 + 3(-4)] \div -4/3$$

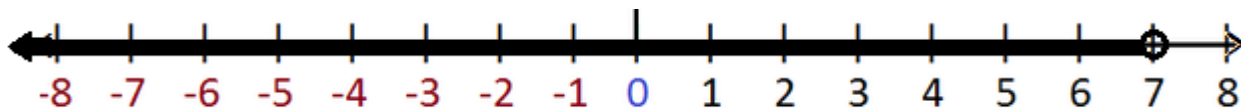
$$[(-8)^2 + -12] \div -4/3$$

$$[64 + -12] \div -4/3$$

$$[52] \div -4/3 = 52 \times -3/4$$

$$= -39$$

(9)  $x < 7$ ;  $-3x + 5 > -16$ ;  $-3x > -21$ ;  $x < 7$ ; for the graph, the domain on  $x$  is all Real numbers.



(10) **86 2/3 ft. or 86.67 ft.**; set up a proportion such as  $26/18 = x/60$  where  $x$  is the height of the apartment building; simplify  $26/18$  to  $13/9$ ;  $13/9 = x/60$ ;  $9x = 13(60)$ ;  $9x = 780$ ;  $x = 780/9$ ;

$x = 86 \frac{2}{3}$  ft. or 86.67 ft.

(11)  $y = \frac{1}{2}x + 14$ ;  $W(-6, 11)$  and  $D(8, 18)$ ; find the slope:  $(18 - 11) \div (8 - -6) = 7/14$  which simplifies to  $1/2$ ; substitute the coordinates of point  $W$  in the equation  $y = \frac{1}{2}x + b$ :

$11 = \frac{1}{2}(-6) + b$ ;  $11 = -3 + b$ ;  $b = 14$ ; the equation is  $y = \frac{1}{2}x + 14$ .

**(12) 2.4 hrs. or 2 hrs. 24 minutes;** Isabella paints at a rate of  $1/6$  of the deck per hr., Elizabeth paints at a rate of  $1/4$  of the deck per hr. Together they paint at  $1/6 + 1/4 = 5/12$ . Use proportion  $5/12 = 1/t$  where  $t$  is the total time together. Solve for  $t$ :  $t = 12/5$ ,  $t = 2.4$  and  $.4$  of 60 minutes is 24 minutes. Algebraically,  $1/6 t + 1/4 t = 1$ ; multiply both sides by 24:  $4t + 6t = 24$ ;  $10t = 24$ ;  $t = 2.4$  hrs. or 2 hrs. 24 minutes.

**(13) (a) The total is  $720^\circ$ ;  $(n - 2) 180^\circ$ ;  $(4)(180) = 720^\circ$ ; (b) Individual angle measure is  $120^\circ$ ;  $720/6 = 120^\circ$ .**

**(14) (a) line d; (b) lines b and f; (c) slope =  $-3/2$  (d) line e; (e) line c; (f) line a**

### Calculator Section Answers

**(15) MAD = 9;** the sum of the bagels for ten days is 1,340 and dividing by 10, the mean is 134 bagels; find the absolute value of the difference between the mean and each bagel amount;  $(0 + 20 + 12 + 7 + 5 + 7 + 22 + 9 + 4 + 4)/10$ ;  $90/10 = 9$ .

**(16) 22 visits;** let  $x$  = the number of visits;  $\$80.00 + \$8.75x = \$12.50 x$ ;  $80.00 = 3.75x$ ;  $80/3.75 = x$ ;  $x = 21.3$  visits but you can't do a fractional part of a visit so the answer must be rounded up to 22 visits. (Students may have used charts or graphs to find the answer.)

**(17)  $y = 5/4 x + 9/2$ ;** also accept answers such as  $y = 1.25 x + 4.5$  or other equivalent equations. In the original equation, the slope was  $-4/5$ ; a line perpendicular to the given line has a slope of  $5/4$  because the product of the two slopes is always  $-1$ ; substitute the coordinates of either point into  $y = 5/4 x + b$  in order to find  $b$ ;  $-3 = 5/4 (-6) + b$ ;  $-12 = -30 + 4b$ ;  $18 = 4b$ ; so  $b = 18/4$  or  $9/2$  or  $4.5$ .

**(18) You will have \$570 at the end of five weeks; yes, you'll have enough money!** \$9.50 times 12 hours equals \$114; \$114 times 5 weeks equals \$570.

**(19) 23 1/3 cups or 23.33 cups;** using proportions,  $4 \frac{3}{8}$  cups of water/1 cup of concentrate is equal to  $x$  cups of water/ $5 \frac{1}{3}$  cups of concentrate;  $x = 4 \frac{3}{8}$  times  $5 \frac{1}{3}$ ;  $35/8$  times  $16/3$  is equal to  $70/3$  or  $23 \frac{1}{3}$  cups or 23.33 cups.

**(20) (a) 240 tiles; (b) the side is 21 1/4 ft. or 21.25 ft.;**  $\$600/\$2.49 = 240.9638554$  tiles which rounds to 240 tiles; for a square patio the largest size would be  $15^2=225$  tiles which is 15 tiles per side; since each square tile has an area of 289 sq. ins., the side length must be 17 inches;  $15 \times 17 = 255$  inches; divide 255 inches by 12 inches (number of inches in a foot) and the answer is  $21 \frac{1}{4}$  ft. or 21.25 ft.

**(21) This is one possible arrangement;** there are other acceptable answers but the sum of all the rows, columns and diagonals, must equal 3.

4	-3	2
-1	1	3
0	5	-2

