## Directions:

- Your answers should be in the form specified in the problem. Approximate answers must be at least three decimal places rounded or truncated (ex: $\frac{2}{3} \approx 0.666$ or 0.667 ), and exact answers must be in simplest form (ex: $\frac{5}{15}$ will not be accepted for $\frac{1}{3}$, and $\sqrt[3]{48}$ will not be accepted for $2 \sqrt[3]{6}$ ). When the desired form is specified in a problem, any other form of the answer will not receive credit.
- You may only use calculators that are permitted on the SAT Tests.
- You may write on this contest and use additional paper you receive from your teacher, but you should write your answers on the Individual Student Cover Page to be official and receive credit.
- You will have exactly 45 minutes to complete the problems in this contest. Work quickly and with accuracy.


## Problems:

1. The dimensions $a, b$ and $c$ of a rectangular prism are in the ratio 3:5:7. If the length of the diagonal is $3 \sqrt{83}$ units, what is the value of $a+b+c$ ?

2. Given positive integers $m$ and $n$ that differ by 35 , such that $m^{2}+n^{2}=2017$.

Find the value of $m+n$.
3. Find the $y$-coordinate of the point on the line $y=2 x+3$ that is closest to the point $(0,7)$.
4. Some values of a function $f$ are shown in the following table:

| $x$ | -5 | -3 | -1 | 1 | 3 | 5 | 7 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | -54 | -20 | -2 | 0 | -14 | -44 | -90 | -152 |

If $g(x)=-\frac{2}{3} f(1-2 x)+f(|x|)$, what is the value of $g(-3)$ ?
5. What is the largest possible number of intersections between eight distinct lines in a plane?
6. If you randomly arrange 5 different math books and 5 different art books on a shelf, what is the probability that you will have two math books at the two ends?
7. Find the exact value of the infinite continued fraction $2+\frac{1}{1+\frac{1}{2+\frac{1}{1+\frac{1}{2+\ldots}}}}$.

8. The peak of a mountain can be seen from points A and B that are both 5,200 feet above sea level, and are 500 feet apart. The angle of elevation at A and B are $20^{\circ}$ and $32^{\circ}$ respectively. Find the elevation from sea level at the mountain peak. Round your answer to the nearest foot.
9. In the figure shown on the right, $\overline{F B}$ is tangent to the circle with center $C$, and $\overline{A B}$ intersects the circle in point $H$. If $A H=7 \mathrm{~cm}$ and $H B=3 \mathrm{~cm}$, find the exact length of $\overline{F B}$.

Figure not drawn to scale

10. How many integer solutions does the inequality $|n-9|<6$ have?
11. In quadrilateral $Q U A D, Q U=21, U A=20, A D=15, U D=25$ and $A Q=29$. Find the area of $Q U A D$.
12. A coin with diameter 1 inch is tossed onto a $24 \times 18$ in $^{2}$ flat surface covered with black and white square tiles as shown. The side of each tile is 3 inches.

What is the probability that the coin lands entirely inside a white tile?

Here's a partial view of the surface:
13. How many points do the graphs of $f(x)=x^{3}+1$ and $g(x)=e^{0.3 x}$ have in common?
14. A look and say sequence is a sequence of integers that begins with a single digit, in which the next term is obtained by describing the previous term.
For example, the sequence starting with the single digit 1 is $1,11^{*}, 21^{* *}, 1211^{* * *}, \ldots$
*there is one 1 in the previous term,
${ }^{* *}$ there are two 1 's in the previous term,
${ }^{* * *}$ there is one 2 and one 1 in the previous term.
The fourth term of this sequence has 4 digits.
How many digits are in the seventh term of the look and say sequence that begins with 2 ?
15. The image shows an equilateral triangle with perimeter 30 units. Each circular arc is centered at a vertex, and has radius that is half the length of each side. Find the exact value for the area of the shaded region with vertices $A, B$, and $C$.


